## **Reconstruction Methods:** Piecing together biochemical reaction networks

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### Outline

- 1) Introduction to reconstruction and genetic circuits
- 2) Reconstructing metabolic networks
  - Components of metabolism
  - Genome annotation
  - Biochemical data
  - Physiological data
  - Mathematical modeling
- 3) Reconstructing regulatory networks
  - Basics of regulation
  - Bottom-up and Top -down Reconstruction
- 4) Reconstructing signal transduction networks
  - Experimental methods
  - Current reconstruction efforts

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#### **REDUCTIONISM REVERSED**

It is thus becoming clear that we need to reverse the process on the left-hand side, and to study how these components interact to form complex systems.

This poses the question, given the complete genomic sequence, is it possible to reconstruct the functions of a cellular or biological system?

The process of reconstructing the biological system from the reductionist information will rely on bioinformatics to identify the "parts catalog" if you will.

However, the parts catalogue does not contain systemic functional information. For example, listing all the parts of a car does not even begin to describe how an automobile works.

Therefore, to understand multigenic functions, a systems science analysis is required.



#### THE CENTRAL DOGMA

This schema illustrates the central dogma of molecular biology **a** it was developed about 40 years ago. The DNA, a long thread like molecule of a specific base-pair sequence, carries the inherited information. Short segments of the DNA molecule (called the open reading frames) are transcribed into a chemical relative, RNA, in the form of a message. This message is then translated into protein, that in turn carry out individual biochemical functions in the cell.

This dogma has been around for many decades. So what is new? What is new is the fact that we can now characterize the entire DNA molecule(s) of an organism in detail, measure all the messages coming from the DNA at any given time, and assay for all the different protein molecules in a cell.

This central dogma is now expanding and being revised. Proteins do not function in isolation. Instead, they participate in multi-geneic functions that comprise cellular physiological behavior. The central dogma of molecular biology is about to be revised and extended through the elucidation of these protein interaction networks and their quantitative systemic characterization.



#### THE DOGMA OF IN SILICO BIOLOGY

As was discussed briefly in the previous slide, the central dogma of molecular biology shows a direct link between protein structure and protein function without regard to protein-protein interactions. Thus we are forced to move beyond the central dogma of molecular biology when trying to reconstruct cellular functions from the component list. First we must identify the pairwise interactions between the individual gene products. Then we must construct the networks that result from the totality of such pair-wise interactions. There are many in vivo and in silico methods currently available to accomplish this task. We will describe some of these in this lecture.

Then we wish to study the properties of these networks. These properties are those of the whole and represent biological properties. Examples include, redundancy, robustness, built in oscillations, etc. These properties cannot be deduced from the components alone.

Some of the methods available for such analysis will be described in subsequent lectures.



#### **BIOCHEMICAL REACTION NETWORK RECONSTRUCTION**

Bioinformatics through genomics is giving us a detailed list of the components found in a cell. We now face the challenge of piecing together how these components interact with one another. For metabolism, this goal is achievable today. Because of the work of dedicated biochemists for over seventy years, a wealth of information exists about metabolism. Thus, for organisms with a sequenced and annotated genome, genome-scale metabolic networks can be reconstructed. It is anticipated that over the next 5 to 10 years we will achieve a similar level of capability with other cellular reaction networks. These will include the reaction networks that underlie cell signaling, as well as cellular fate processes such as apoptosis, mitosis, and differentiation. Bioinformatics is thus beginning to move from the enumeration and characterization of individual components to piecing together the interactions between them, ultimately defining these reaction maps in great detail.



#### **GENETIC CIRCUITS**

The relationship between the genotype and the phenotype is complex, highly non-linear and cannot be predicted from simply cataloging and assigning gene functions to genes found in a genome.

Since cellular functions rely on the coordinated activity of multiple gene products, the inter-relatedness and connectivity of these elements becomes critical.

The coordinated action of multiple gene products can be viewed as a network, or a "GENETIC CIRCUIT," which is the collection of different gene products that together are required to execute a particular function.

Therefore, if we are to understand how cellular functions operate, the function of every gene must be placed in the context of its role in attaining the set goals of a cellular function.

This "holistic" approach to the study of cellular function centers around the concept of a genetic circuit, and is the philosophy behind much of the material in these notes.

The skill set that is required to carry out the integrative approach is quite different than the skill set required for the reductionistic approach. It comes down to understanding information technology, systems science analysis, mathematical modeling and computer simulation. This skill set currently is scarce and the material in this class is focused on developing those skills.



#### CLASSIFICATION OF GENETIC CIRCUITS

There are hundreds, and potentially thousands of genetic circuits found on animal genomes. We can coarsely classify them into 3 categories.

•1. Circuits that deal with mass and energy handling in the cell. These genetic circuits describe metabolic and transport activity in cells. Typically, about one-third of the genes found on a genome relate to this activity. Understanding the function of the metabolic genetic circuits is fundamental to the field of metabolic engineering.

•2. Circuits that deal with the processing of information. Information processing in a cell includes the information found in the DNA base sequence, and how that information is transcribed, translated, and controlled. The manipulation of these processes underlies the engineering of cells, such as engineering cell clones for the production of a particular protein.

•3. Circuits that deal with the cellular fate processes in multi-cellular organisms. These are the genetic circuits that drive apoptosis, mitosis, cell differentiation, and so forth. This interaction between cells is fundamental to understanding the dynamic functions of tissues and the engineering thereof. It should be noted that within this paradigm, gene transfer for gene therapy represents the re-tuning of a malfunctioning circuit. Designing these circuits from scratch is unlikely to ever occur since much fine-tuning has taken place through the evolutionary process.

### **Properties of Genetic Circuits**

#### Characteristics:

- They are complex
- They are autonomous
- They execute particular functions
- They are flexible and redundant
- They have "emergent properties"
- They are conserved, but can adjust

#### Analysis methods:

- Bioinformatics
- Control theory
- Transport and kinetic theory
- Systems science
- Bifurcation analysis
- Evolutionary dynamics

### Informatic, P/C, and biological properties

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#### **PROPERTIES OF GENETIC CIRCUITS**

Genetic circuits have many interesting informatic and physico-chemical properties, some of which are outlined on this slide. First, they are complex, and tend to be comprised of a few dozen gene products. The complexity of genetic circuits will be analyzed through bioinformatics and is fundamentally an IT problem. Secondly, gene circuits have physical-chemical properties. Once expressed, they are autonomous and function in response to their environment. For instance, glycolysis, once expressed, when exposed to glucose will metabolize glucose to lactate. It does so in a self-controlled manner. In other words, the interactions of the gene products at this level have a built-in control and regulatory structure. The gene products execute particular functions such as cell migration, transport of molecules in a vesicle, and so forth. These processes could be described by basic transport phenomena and kinetic theory.

Genetic circuits also have some very interesting biological properties. First they are very flexible and redundant. One can remove components of the circuits and they still maintain their function. Second, they have emergent properties. These are properties that emerge from the whole and are not derivable from the properties of the individual parts. Such properties are analyzed mathematically by a branch of mathematics known as bifurcation analysis. Finally, genetic circuits, once established, are conserved with evolution. For instance, once glycolysis was developed, it stayed with cells throughout evolution and is found now in essentially all cells. Another example are the genes that lay out the basic body plan that decides where the head, arms, and legs are, and so forth. It has been shown for instance, that a human circuit that lays out the body plan can be put into the fruit fly, and will function relatively normally. So the circuits that lay out the body plan are conserved. In other words, the basic biochemical process may have been conserved, but how they are regulated and integrated into other cell functions is highly organism-specific. Evolutionary dynamics are responsible for how these genetic circuits adjust over time.

## Two Key Steps

- Reconstruction of Networks
  - Methods
  - Network characteristics
  - The reconstruction process
- Mathematical Modeling of Networks
  - Topological
  - Steady state
  - Dynamic

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#### THE COMPONENTS OF A CELL

These basic cellular components are familiar to most students. Cells basically have three major groups of macromolecules: proteins, nucleic acids, and polysaccharides. In addition, fats and lipids are a major class of molecules in cells. Cells also have a number of small molecules that can be organic or inorganic. The organic small molecules are thevarious metabolites. Some of these small molecules serve as the building block for the macromolecules. Proteins are made from amino acids, nucleic acids are made from nucleotides, and polysaccharides are made from sugars.



#### THE APPEARANCE OF CELLULAR COMPONENTS

An insightful book has been published by David Goodsell called 'The Machinery of Life' in which he draws the size and shape of the different cellular components to scale. The relative sizes and shapes of these cellular components are very useful for the visualization of the intracellular processes shown on this slide. For example, the size of the ten enzymes of glycolysis (1) can be compared to the size of glucose(b) to gain an understanding of the size of a protein relative to a metabolite on which it acts.

For those interested, David Goodsell has also published a great sequel to 'The Machinery of Life,' called 'Our Molecular Nature.'



#### **ENZYMES AND SUBSTRATES**

This slide shows what a metabolic gene product actually looks like. Shown here is hexokinase, the first enzyme in glycolysis. This complicated protein has an active site on which the actual chemical **catalysis** takes place. The conversion of glucose to glucose-6 phosphate by using a phosphate group from ATP is shown in the insert on the slide. ADP is formed in the process.



#### **GENETIC CIRCUITS**

Within this complex intracellular milieu, with a relatively low number of each type of molecule, the genetic circuits operate. The process of protein synthesis is illustrated in this slide. All the components involved in this process including the ribosome and its subunits, the mRNA, the tRNA, and so forth, are shown here. All of these must come together to translate the information on the mRNA into a protein sequence. The process of protein synthesis operates at a high speed of about 15 amino acids per second in the intracellular milieu. There are several of these molecular machines at work in *E. coli* at any given time, and all of them function flawlessly in this complex intracellular environment.

Can you imagine how this complex process can be described in mathematical detail?



This is one more way of looking at the paradigm shift which has taken place in the biological sciences. In the 20th century, biological science focused on reductionism, and emphasized classification categorization, which is essentially breaking the system down into manageable components, and investigating the components in detail. Now, with computational tools and availability of completed databases, we are in the position to reconstruct the overall network from components.



In constructing a metabolic model, one begins by collecting all of the relevant information about an organism. Then one may add reactions to our network based on direct evidence, such as finding a gene in the genome annotation or finding legacy data where the protein is examined experimentally. Indirect cell physiological evidence, such as the known ability of the cell to produce an amino acid in vivo, may lead us to include reactions which "fill in the pathway" to produce that amino acid. These reactions combine to produce a metabolic reconstruction. Our next goal is to expand this network so that it can simulate cell behavior. For this, the network must be able to produce or take up all of the necessary components of a biomass. We add the reactions necessary to fulfill the biomass requirements and call them "inferred reactions." This set of reactions comprises the metabolic model when combined with quantitative analytical methods, which enable us to simulate cell behavior and generate new predictions about the emergent properties of the system. These are properties which emerge from the whole system and are not properties of the individual parts.





All of the reactions in our bacterial models take place in either the cytosol or the extracellular space. However, when reconstructing metabolism in an eukaryotic organism, we must consider other intracellular compartments found within the cytosol. For example, there are 8 compartments included in our yeast model. In addition to the extracellular space and cytosol, these include the **nucleus**, which is the site of DNA replication, transcription and RNA processing; the **mitochondria**, where ATP is synthesized by oxidative phosphorylation; the **vacuole**, a storage compartment for various components, such as food particles and water; the **Golgi apparatus**, where proteins and lipids are modified, stored, and packaged; the **peroxisome**, where toxic compounds are degraded; and, finally, the **endoplasmic reticulum**, where many proteins are synthesized and modified, along with some lipid synthesis.

Developing a multi-compartmental models highlights the fact that some of the compartments are less wellcharacterized than others. For example, experimental studies may show that an enzyme is localized to the membrane of endoplasmic reticulum, but it is unknown whether the catalytic site of this enzyme faces the lumen or the cytosol. In addition, even when parts of a pathway are known to occur across several organelles, there may be little information available on the localization of the compounds and how they are transported between compartments. Thus, a compartmentalized model may require us to infer these transport reactions.

Finally, compartmentalization introduces another level of complexity in maintaining a cell's energy balance. Unlike the bacterial cell, where all of energy production and usage occurs in the cytosol, a eukaryotic model requires energy balance within each compartment. For instance, NADH and NADPH must be produced and consumed as needed to balance the redox potential within a compartment. ATP and protons also have an impact on the cell's energy potential, and these metabolites must also be balanced within the compartment if they have no means of being transported across its membrane.



ORFs are first identified, then assigned a function to each gene. This can be done through experimental methods (cloning, knockout), or by using sequence homology to inferred functions. These *in silico* methods can uncover 40-70% of genetic functions. As explained earlier, there are also many new methods for genome annotation. For example, functions may be inferred from protein-protein interactions, transcriptomics, phylogenetic profiles, protein fusion, and operon clustering (for eukaryotes), to name but a few. The automation of network reconstruction has also been developed to some extent, as will be discussed later.

Year	1997 <sup>1</sup>	2001 <sup>2</sup>	Every gene annotation is sin
Genes	4,404	4,401	a hypothesis whi
Known	2,178	2,233	must be continua
Putative	594	1,306	re-evaluated
Unknown	1,632	862	
<ol> <li>Blattner, F. R. <i>et al.</i> The complete genome sequence of <i>Escherichia coli</i> K-12. <i>Science</i> 277, 1453-74 (1997).</li> <li>Serres, M. H. <i>et al.</i> A functional update of the <i>Escherichia coli</i> K-12 genome. <i>Genome Biol</i> 2 (2001).</li> </ol>			However, the ger can be cloned and functionally characterized

It can hardly be emphasized enough that every gene annotation is hypothetical and that annotation will always have to be re-evaluated. One example is E. coli, whose annotation was recently updated by the Riley lab. As you can see, the newer version of the annotation has fewer genes, but more known and putative genes. Additionally, for some genes the functionality often must be re-assigned. In other words, the annotation of a genome is far from being the "last word", and in fact, as will be shown later in this lecture, model reconstruction is a powerful way of both curating a network and directing research in a powerful way to facilitate annotation and discovery.



There are several interesting databases around which give access to genomic data. One of my favorites is the Comprehensive Microbial Resource (CMR), which currently provides tools for the analysis of 63 annotated genome sequences, both singly and together. The Institute for Genomic Research (TIGR) maintains this site very well and I used it as the main site when putting together the H. pylori model.



One interesting way KEGG organizes its genomic information is by using these reaction network "maps." The above map shows glycolysis. Arrows connect various metabolites to each other, indicating that one metabolite can be converted to another in a reaction. The boxes which stand beside the arrows are the enzymes which catalyze these reactions.

KEGG is another important network reconstruction database with genome annotation. It uses the same maps for many organisms, so not all of the pathways shown in this map are actually available for *H. pylori*. Some are for *E. coli*, for example. The genes actually found in *H. pylori*, according to this map, are the ones which are highlighted in green. This visual presentation method makes it easy to see at a glance which genes appear to be missing from the genome and also to compare organisms. Although there is a lot of interface between databases such as KEGG and TIGR, I generally use KEGG primarily for organizational purposes and TIGR for my actual genome annotation.



The next set of important data to integrate into our models is biochemical data, which focuses on reactions, their stoichiometry and whether or not they are reversible. For example, the enzyme which catalyzes the above reaction, D-Glucose converting to D-Glucose-6-phosphate as ATP is converted to ADP, is called Glucokinase. The gene which encodes this enzyme is commonly called glk, and the E.C. number which corresponds to the reaction is 2.7.1.1. A picture of the Human beta cell glucokinase structure is shown on the right (found in the Protein Data Bank).

If we were trying to determine whether or not glycolysis occurred in *H. pylori*, we would search KEGG and TIGR for the relevant genes. The gene *gl*k would be found in both of these databases. Once this gene had been positively identified, preferably by both web-based sources, we would add the enzyme that this gene encodes and include its corresponding reaction to our model.



When assigning genes to reactions and vice versa, it is important to remember that not all genes have a one-to-one relationship with their corresponding enzymes or reactions. For example, many genes may encode subunits of a protein which catalyzes one reaction. A beautiful example of this is the fumarate reductase shown at the right. There are four subunits, frdA, frdB, frdC and frdD, without which the protein will not be able to catalyze its reaction.

On the other hand, there are genes which encode so-called "promiscuous" enzymes which catalyze several reactions, such as transketolase I in the pentose phosphate pathway. This gene product catalyzes the two reactions shown.



Some of you may have wondered what E.C. numbers are. They have been established to specify enzyme reactions unambiguously. This is essential because so many reactions have ambiguous names. To prove this to yourselves, try going to the E.C. website and searching, first for succinate dehydrogenase and then for fumarate reductase. Both of these enzymes catalyze the same reaction, but in opposite directions. Some biochemists find that frd or sdh may be reversible at times. As a result, when you type in succinate dehyrogenase you will find that it is often used to indicate either reaction. Gene names have similar problems.



The enzymologists should be complimented for this effort, as it greatly simplifies our efforts. Eventually similar nomenclatures will have to be worked out for all proteins in the cell. Dr. Milton Saier has already initiated the process with T.C. numbers for transport proteins; however, much remains to be done.

Another point is that because they are unique, once E.C. numbers have been connected with reactions in one organism, the resulting assignment may be linked to any other reconstruction effort where the organism is thought to catalyze the corresponding reaction. Because they are standardized numbers, you can trust them to be the same across multiple organisms.



The important next step for biological databases will be to integrate genome and biochemical data. One site that has done some of this is the EcoCyc database, which incorporates some biochemical knowledge. Here is a frame from the site. You can click on enzymes in these pathways to obtain more information about their properties. EcoCyc is one of many organismspecific databases which can help you; MIPS and YPD are two examples for yeast. Search the Internet to locate databases for your particular organism.

# Organism-specific Textbooks



- Great starting point
- Broad view of the organism's metabolism, biochemistry, physiology, uses, etc.

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Finally, it should be mentioned that for many of the organisms of interest, fairly comprehensive textbooks have been written which include detailed descriptions of the organisms' metabolism. These books will give you an overview of the organism's importance, metabolic features and important references, as well as physiology. I still use the E. coli 2 volume set even in building models for other organisms, as it is the best-characterized model prokaryote. (Note that "EcoSal", a web-based and updated version of the Neidhardt classics, is due out in the next few months!)



Literature searches are probably a basic to many of you, but they are covered lightly here because (1) they are vital to this kind of research and (2) most people don't search as efficiently as they could – there is always more to learn! The searches are vital because in constructing a network you will need as much data as you can find. Some tips are listed here; for more, look at the "Preview/Index" tab in PubMed.



So why do we need biochemical data? Although the model has been mostly determined using various computer databases to find annotated genes, it is not yet complete. Careful study will show the absence of enzymes catalyzing reactions which most likely occur in the thriving organism. In these cases, where the enzyme has not yet been identified, we review the relevant literature to see if various research groups have determined the presence or absence of particular enzymes. For example, in the above case, both KEGG and TIGR give no indication that phosphofructokinase is found in *H. pylori*. This could mean that *H. pylori* is not able to produce 1,6-Fructosebisphosphate (FDP) from Glucose, although there may be other pathways by which FDP is produced. Careful review of the literature reveals that the Phosphfructokinase enzyme may have been identified by Hoffman et. al. in 1996. Other scientists, however, dispute this claim. After thoroughly examining studies of H. pylori metabolism, we will decide whether or not to include this enzyme and the reaction it catalyzes into our model. Biochemical data is therefore fundamental to both curating and expanding the network.



Even after we have searched the on-line databases and all of the relevant literature, there is still a high probability that several necessary reactions will be missing from the model. This is because the ORFs for the genes in the genome have not yet been identified and/or linked to these reactions. This is one of the most exciting parts of building a model, because we will decide, based on our own knowledge of how *H. pylori* grows, whether a gene is present simply because it must be present to for *H. pylori* to function as has been determined experimentally. By "filling in the gaps" in this way, we have the potential to drive further genomic research, determining the presence of genes *in silico*.

	Amir	Amino Acid Requirements		
Experiments determine	AA	Reynolds	Model	
which amino acids are	Ala			
which amino actus are	Arg			
taken up by <i>H. pylori</i> vs.	Asn			
	Asp Cys	+++++++++++++++++++++++++++++++++++++++		
which can be produced <i>in</i>	Gln			
vivo	Glu			
	Gly			
Missing steps of amino	His			
	lle			
acid biosynthesis are	Leu			
added if necessary on the	Lys Met	+	+	
•	Phe			
basis of this	Pro			
physiological evidence	Ser			
phijotoblear e Haenee	Thr			
	Тгр			
	Tyr			
	Val			

One example of this process is shown here. The chart shows the amino acid requirements of *H. pylori*, as determined in vivo (left) and in silico (right). A '-' indicates that the organism can not grow without this amino acid; a '+' indicates that the amino acid is synthesized in vivo. If the physiological data indicates that the amino acid is synthesized by the organism but the pathway (as based on genomic/biochemical data) is incomplete, then we add the necessary steps – very tentatively – on the basis of this indirect physiological evidence.

<b>Biomass Composition</b>					
<ul> <li>Indicates demands of the system (more detail in modeling section of class)</li> <li>Precursors may also be used for smaller networks</li> </ul>	Metabolite ATP NAD <sup>+</sup> NADPH G6P F6P R5P E4P GA3P 3PG	OII Demand (mmol) 41.3 3.5 18.2 0.2 0.1 0.9 0.4 0.1 1.5			
<ul> <li>Approximation of Biomass composition for less-characterized organisms (<i>H. pylori</i>, <i>H. influenzae</i>)</li> <li>University of California, San Diego Department of Bioengineering</li> </ul>	PEP PYR ACCOA OXA AKG SUCCOA	0.5 2.8 3.7 1.8 1.1 (trace) Systems Biology Research Group http://systemsbiology.uesd.edu			

There are other important physiological data to consider and find if possible. One is the Biomass composition of the organism. This is particularly important for the models constructed as part of the Genetic Circuits Research Group, as we assume for the purposes of our models that the network must be able to synthesize or transport all biomass components. Sometimes the precursors of growth may be used for simulation of smaller networks. In many cases the biomass composition of an organism will not be available; for these, the biomass composition of a closely related organism may be used – for example, in modeling H. pylori and H. influenzae we assumed a biomass composition similar to that for E. coli. This would not be acceptable in modeling S. cerevisiae. Obviously, the best option is to experimentally determine the composition for the organism of interest.



Finally, it is important to obtain physiological data to try and benchmark or test your model. Can your reconstructed network reproduce simple physiological behaviors which have been observed experimentally? If not, it needs to be improved! I've included an example which shows time course growth, transcription, uptake and secretion data which has been compared to *in silico* predictions. The agreement we see here leads me to trust the model in this circumstance. If there wasn't agreement, I would go back and try to determine why, incorporating any new findings into the model. In many ways this process of benchmarking and iteratively improving the model is the *beginning* of constructing a model, just as going over the first draft of a paper is the *beginning* of writing. This step takes the most time and the most thought.



I mentioned at the beginning of the lecture that some reactions are included in these models based on modeling considerations rather than any experimental or genomic evidence. We call these the "inferred" reactions because they are inferred based on indirect physiological evidence. One example relates to the biomass composition. As mentioned earlier, we assume that the cell must be able to produce all biomass components to grow for modeling purposes. If a cell can not transport or synthesize necessary components, the necessary reactions must be added. These are often transport proteins. The inferred reactions are of course the most tentative in the model and should definitely be examined with the most scrutiny.


By now it is clear that not all reactions in the reconstruction are included with the same confidence levels. Obviously the reactions in which we are most confident are those which have been demonstrated by direct experimentation – biochemical evidence. We trust in the genome annotation and the physiological data somewhat less emphatically and the inferred reactions hardly at all. The best way to build confidence in a reaction is to see if you can find multiple types of evidence to support your assertions.



For an example, let's say we wanted to model traffic patterns in the city of San Diego, analogous to modeling flux distributions in a cell culture. One way to start would be by characterizing each road in detail. This would give us a list of "parts" or functions and would tell us interesting things about the components, such as a large or small road, the speed limit, etc. However, we would not be able to say anything about the integrated function of these parts.



The next step would be to integrate these components into a "map" – whether a road map or a metabolic map. This enables us to tell some things about the system – can I get to Horton Plaza from UCSD? Can H. pylori make pyruvate given glucose in the environment? – which deal mostly with qualitative and/or primarily topological issues. However, such a map can *not* simulate network behavior. For example, you can not tell the travel time from a road map.



Just a network alone isn't enough. For quantitative analysis purposes, using freeway traffic as analogy, a roadmap can tell if a path exists from  $A \rightarrow B$ , but couldn't determine the travel time or volume. One needs to know factors like weather, road conditions, time of the day, etc. Similarly to model cell behavior we need to incorporate many of the external factors which affect cells.

However, to carry the analogy a bit further, anyone who has lived in San Diego for a while may somewhat easily predict travel time from A to B based on a few more important parameters (e.g. time of day, approximate weather conditions) within a factor of 2. This shows that not all the parameters need necessarily be known to have a good phenotypic model. Similarly, you will see later in the course that some of the details of the cellular "parts list" (such as kinetic information) are neglected so that systemic behavior may be described at a genome scale.



Topic 9 describes the process of reconstructing regulatory networks at the genome scale, which is a relatively new field even by "post-genome age" standards.



#### **BASICS OF REGULATION**

There are two subtopics we will cover: first, the basics of regulation for a general background, and then we will talk specifically about reconstruction. So, what is regulation and how does it affect cellular behavior? We will answer this question first, by addressing the importance of accounting for regulation in our models. Next we will give a brief primer on regulation, beginning with types of cellular regulation, a description of transcriptional activators and repressors, some differences in regulation between prokaryotes and eukaryotes, and then mention some common types of transcriptional regulation exhibited by microbes.

Why do we Care About Regulation?			
Regulation has a significant	Distribution of E. coli proteins among 22 functional groups (simplified schema) (Blattner et al.)		
	Functional class Metabolism	Number	% of total
effect on cell behavior	Central intermediary metabolism	188	4.4%
<i>cjj cet en cen c</i> entric.	Carbon compound catabolism	130	3.0%
	Amino acid biosynthesis and metabolism	131	3.1%
	Nucleotide biosynthesis and metabolism	58	1.4%
Example: E. coli	Fatty acid and phospholipid metabolism	48 103	1.1%
	Biosynthesis of cofactors, prosthetic groups and carriers Energy Metabolism	243	2.4% 5.7%
-Estimated 400 regulatory genes	Putative enzymes	243	5.9%
	Total Metabolism	1152	26.9%
	Transport		
	Transport and binding proteins	281	6.6%
-178 regulatory and putative	Putative transport proteins	146	3.4%
regulatory genes found in genome	Total Transport	427	10.0%
regulatory genes found in genome	Regulation Regulatory function	45	1.0%
(1 <sup>st</sup> pass)	Putative regulatory proteins	45	3.1%
(1 pubb)	Total Regulation	178	4.2%
	Structure		
	Cell structure	182	4.2%
-690 transcription units (contiguous	Putative membrane proteins	13	0.3%
	Putative structural proteins	42	1.0%
genes with a common expression	Total Structure Macromolecules	237	5.5%
condition, promoter and terminator)	DNA replication, recombination, modification and repair	115	2.7%
	Transcription, RNA synthesis, metabolism and modification	55	1.3%
identified in RegulonDB	Translation, posttranslational protein modification	182	4.2%
	Total Macromolecules	352	8.2%
	Phage, transposons, plasmids	87 188	2.0%
	Cell processes (including adaptation, protection) Putative chaperones	188	4.4% 0.2%
–Will affect model predictions	Other known genes	26	0.2%
	Hypothetical, unclassified, unknown	1632	38.1%
	Total	4288	100.0%
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#### WHY REGULATION?

To begin: why do we care about regulation? When building a mathematical model it is as important to know what one can *neglect* in a model as it is to know what to *include*. Can we neglect regulation? The answer is, perhaps under some conditions, but certainly not in all cases. The reason is that regulation has a significant effect on cell behavior. As an example I have shown here a table in which *E. coli* proteins where distributed among 22 functional groups (from the first-draft K-12 annotation). You can see how metabolism and transport accounts for a substantial number of the known genes. Additionally, it is estimated that 400 (~10%) of the genes in E. coli have transcriptional regulatory functions; of these 178 regulatory and putative regulatory genes have been found in the genome. According to RegulonDB, a database we will discuss in more detail later, there are 690 transcription units (e.g. regulated genes or operons) which have been identified in this organism. Modeling these units will have a major effect on model predictions where regulatory effects have a dominant influence on metabolism. I'll add in passing that the effect of regulation is generally much greater in eukaryotes.



#### LEVELS OF REGULATION

When we say "regulation" we could be including any of a number of regulatory processes implemented by cells, illustrated schematic ally here. Cells can regulate their behavior at the gene, mRNA transcript, protein, protein activity and metabolite level. For the purposes of this discussion we are considering primarily *transcriptional* regulation, which is at the gene level. In other words we are considering the case where a stimulus is sensed and the response is induction or repression of transcription of one or more genes in the DNA. The changed concentration of the corresponding protein results in a new state and possibly a new behavior of the cell.



#### **RECONSTRUCTING REGULATORY NETWORKS**

That concludes our overview of transcriptional regulation. Our next subtopic is constructing regulatory networks. How can we reconstruct metabolic networks and integrate them with what we know about metabolism? In covering this topic, we will compare regulation to metabolism and discuss how we can adapt our metabolic network reconstruction methods to regulatory network reconstruction, sometimes called the "bottom-up" approach because we are building the network from the known parts. There is also a so-called "top-down" approach to reconstructing these networks, which attempts to infer the network from the transcriptomics data. We will give you a brief introduction to that approach as well and finish with a few statements about modeling regulatory and combined metabolic/regulatory networks.



This diagram shows how we reconstruct regulatory networks, and you will notice that the process is similar in concept to the process of metabolic network reconstruction. Again, we need to draw together the genomic, biochemical and physiological data, inferring functions where necessary. However, in this case (for bottom-up reconstruction) we will rely mostly on biochemically characterized regulatory proteins and their corresponding genes. Rather than including metabolic reactions, we will include *regulatory rules*, for example "gene *abcD* is transcribed if regulatory protein ProT is active" and "regulatory protein Prot is active if there is oxygen in the extracellular environment". These rules can be represented using Boolean logic, kinetic theory and the like.

The metabolic network may be constructed as usual and now the two networks may be analyzed separately or together with analytical methods as a metabolic/regulatory model. Once again, such a model will make predictions about the behavior and emergent properties of the system which should be seen as hypotheses which must be tested experimentally.



#### **BOTTOM-UP RECONSTRUCTION**

However, it is possible to reconstruct regulatory networks, given the information we have, and the process is similar in concept to the process of metabolic network reconstruction. Again, we need to draw together the genomic, biochemical and physiological data, inferring functions where necessary. However, in this case (for bottom-up reconstruction) we will rely mostly on biochemically characterized regulatory proteins and their corresponding genes. Rather than including metabolic reactions, we will include *regulatory rules*, for example "gene *abcD* is transcribed if regulatory protein ProT is active" and "regulatory protein Prot is active if there is oxygen in the extracellular environment". These rules can be represented using Boolean logic, kinetic theory and the like.

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# Description regulatory information? Stranscription regulation Boolean (switch-like) or continuous? (Biggar SR and Crabtree GR EMBO J 20:3167 (2001)) Should transcription be thought of as a stochastic or determinis tic process? What constitutes significant regulation? Many extracellular signals can affect expression level of a gene Which signal are actually physiologically significant? Experiments done under different conditions (e.g. strain background). Typically experimentalists concentrate on studying well-known fylarget pairs in great detail

#### **ISSUES IN REGULATORY RECONSTRUCTION**

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Because reconstructing regulatory networks in the genome (or in fact any) scale is such a young field there are still many unresolved issues. A major issue is how regulatory information should be represented – this is especially relevant with regards to what type of models are built based on the regulatory information. In these slides as well as in most of the genetics literature the assumption is usually made that a gene is either transcribed or not, i.e. regulation is assumed to be switch like (or Boolean). However, it is well known by biochemists (but maybe not by geneticists?) that regulatory processes are in essence no different from other biochemical processes and that different magnitudes of incoming signals can cause different levels of transcriptional activity. This issue is illuminated in the following paper: Biggar SR, Crabtree GR

# **Cell signaling can direct either binary or graded transcriptional responses.** EMBO J. 2001 Jun 15;20(12):3167-76.

Another issue relevant to regulatory reconstruction is what is considered to be a significant regulatory interaction. In many cases multiple signals can regulate the transcription of one gene, but some of these signals only play a modulatory role. These signal are not capable of changing transcriptional activity on their own and only act in the presence of other stronger signals. A third problem is how experimental data in the literature should be interpreted. For example studies on transcriptional regulation *in vitro* may not be very useful, because they do not account for other regulatory signals present *in vivo*.



#### **TOP-DOWN RECONSTUCTION**

In addition to the issues discussed in the previous slide that are common to any approach to reconstructing and modeling regulatory networks there are a couple of specific problems with the bottom-up (literature-based) approach. The first is due to the fact that up to very recent years targets for transcription factors were usually identified one gene at a time. While this ensures very low false positive rates, it also means that most relevant targets for many transcription factors have not been identified. The second problem is the general lack of structured databases on transcriptional regulation, which makes the actual reconstruction process exceedingly time-consuming.

An alternative approach to the bottom-up approach has emerged in the last few years primarily due to the availability of large-scale gene expression profiling data. This approach, which we call top-down reconstruction, is based on the idea that since we know the "outputs" of the complex regulatory circuit in the form of gene expression profiles, we should be able to reconstruct the underlying circuit solely from this data. Although gene expression data clearly is useful for this task it is not the only type of data that could potentially be utilized. Additional useful data sets are location analysis (or ChIP-Chip) data, which describes genome-wide binding sites of TFs, and promoter sequence data (the region upstream of the transcription start site), which can be used to computationally identify binding sites for transcription factors.



#### METHODS FOR TOP-DOWN RECONSTRUCTION

The overall goals of the top-down reconstruction process is to integrate and synthesize all the data sets described in the previous slide and use the integrated data set to: (1) Predict new targets for TFs (or describe the network structure) ane (2) Predict the strength/direction of regulation for each TF/target pair (or estimate/fit model parameters).

There have been many different approaches proposed for the top-down reconstruction task. Each approach is based on proposing a different type of model for the regulatory network and developing methods for fitting the model to the observed data. Typical approaches include: (1) Dynamical systems models (e.g. linear and nonlinear models) for with the model fitting is known as systems identification, (2) Boolean network models where the model fitting is usually done by searching through the space of possible network structures using combinatorial approaches, and (3) Bayesian network models (or more generally graphical statistical models), which will be described in more detain in the next slide. de Jong H

Modeling and simulation of genetic regulatory systems: a literature review.

J Comput Biol. 2002;9(1):67-103

D'haeseleer P, Liang S, Somogyi R

Genetic network inference: from co-expression clustering to reverse engineering.

Bioinformatics. 2000 Aug;16(8):707-26.

Segal E, Barash Y, Simon I, Friedman N, Koller D

From Promoter Sequence to Expression: A Probabilistic Framework

Proceedings of the 6th International Conference on Research in Computational Molecular Biology (RECOMB) 2002



#### **BAYESIAN NETWORK APPROACHES FOR TOP-DOWN RECONSTRUCTION**

Actually all the modeling strategies described in the previous slide can be considered to be a subclass of a general statistical modeling framework – graphical models. Bayesian (belief) networks are a particular type of graphical model that can be used to describe conditional independence relations between expression levels of genes (typically discretized e.g. to a binary representation of gene expression). These networks are a very natural representation for regulatory circuits, where there is uncertainty associated with both the network structure and parameters due to both biological and experimental noise in the available data. There are two main features to a Bayesian ne twork – network structure and parameters can be learned from data, but learning structure is much more difficult than learning parameters given a structure (see Murphy and Mian 1999). However, in most reconstruction approaches network structure is exactly what one wants to find and hence different kinds of optimization approaches have been used to search for the best structure given the data (see papers below for two approaches).

Friedman N, Linial M, Nachman I, Pe'er D

Using Bayesian networks to analyze expression data.

J Comput Biol. 2000;7(3-4):601-20.

Hartemink AJ, Gifford DK, Jaakkola TS, Young RA

**Combining location and expression data for principled discovery of genetic regulatory network models.** Pac Symp Biocomput. 2002;:437-49.

Murphy K and Mian S

Modelling Gene Expression Data using Dynamic Bayesian Networks

UC Berkeley CS Technical Report 1999

http://www.cs.berkeley.edu/~murphyk/papers.html

# Issues with top-down reconstruction

- Very complex models and algorithms are required to reverse-engineer regulatory circuits
  - Computational issues: Explosion in the number of structures
  - *Model complexity* issues: Explosion in the number of parameters
  - *Optimality* issues: Only locally optimal circuits can be found
- Data is not usually available in sufficient quantities or with appropriate quality computational and experimental people usually don't work together
- Most models require discretizing gene expression data
- Currently these methods are primarily used to create hypotheses about potential targets of TFs

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#### **ISSUES WITH TOP-DOWN RECONSTRUCTION**

In addition to the issues mentioned in conjunction with the bottom-down reconstruction approach, the top-down approach suffers from its own weaknesses. The major problem is that since the underlying regulatory circuit is potentially very complex, the types of models and algorithms required for top-down reconstruction also tend to be very complex (in fact these are probably some of the most complex statistical models ever constructed). While this complexity is not a problem as such it results in a few practical problems in fitting the model that are detailed in the slide. A central problem is the explosion in the number of different alternative models (both structure and parameters) to be considered, which requires both large amounts of sufficiently high-quality experimental data and efficient methods for learning models from data. Recently, however, some of the best statistical modeling people have started collaborating with some of the best biology groups that are capable of generating large quantities of high-quality data. This should lead in rapid improvement in both the methods for top-down reconstruction and in new biological knowledge from the reconstruction efforts.



#### COMBINED REGULATORY AND METABOLIC MODELING

Here is another sneak preview, showing what kinds of calculations are possible using the regulated flux balance approach and the regulated *E. coli* metabolic network in a simulation of the glucose-lactose diauxic shift mentioned earlier. Using this approach it is possible to generate time courses of growth as well as glucose and lactose uptake. It is also possible to infer concentrations of proteins and even to simulate, qualitatively, gene expression data. We can also simulate the effects of gene deletions on cellular behavior with more accuracy and broader scope.





Signal transduction is a broad field of cell biology. It involves the "transduction" of a "signal" from the outside of the cell to the inside of the cell. When the cell encounters an extra cellular signal (i.e. the binding of a growth factor to an extracellular receptor) a sequence of events takes place. These can be as simple as the opening of an ion channel (i.e. acetylcholine triggers the influx of calcium ions) or as complex as a highly interconnected network of protein phosphorylations. In brief, signal transduction often involves the following steps: (1) the binding of a ligand to an extracellular receptor, (2) the subsequent phosphorylation of an intracellular enzyme, (3) amplification and passage of the signal, and (4) the resultant change in cellular function (i.e. up-regulation of a gene).

Various classification schemes exist for the different components of signal transduction.



The mechanisms of signal transfer are often grouped into three categories: (1) soluble molecules like growth factors and chemokines are secreted from one cell and received by another, (2) cell and extracellular matrix interactions form another class of signal processing. An example of this type can be seen in the cells involved in blood vessels. Stresses and strains experienced by these cells can be sensed through integrin bonds to extracellular matrix proteins. (3) Cell-cell interactions involve signals like ion movement. This is often seen in cardiac tissue as a depolarization (which leads to muscle contraction) of one cell and then is passed on to another.



There are also three classes of receptors involved in signal transduction: (1) G protein-coupled receptors, where a receptor is coupled to an intracellular GTP binding and hydrolyzing domain, (2) ion-channel linked receptors, where a bound ligand triggers the opening of an ion channel, and (3) enzyme-linked receptors, where the receptor also has an enzymatic domain such as tyrosine kinases.

With this background, we can now look at what efforts are underway to reconstruct signaling networks.

## Experimental methods genomic approaches

#### • DNA microarray expression profiling

- Determine input/output relationships (e.g. in the presence of particular ligands, what genes are up/down-regulated)
- Roberts, et al. (2000) Science, 287: 873-880

#### • ChIP (chromatin immunoprecipitation) chip

- Cells lysed with transcription factors bound to appropriate DNA
- DNA fragments with bound TFs are immunoprecipiated
- Bound DNA fragments are recovered, labeled, and hybridized to a DNA chip
- Identifies all bound targets
- Ren, et al. (2000) Science, 290:2306-2309

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# Experimental methods proteomic approaches

- Yeast two-hybrid screens
  - Protein of interest is fused to a DNA binding protein
  - Target proteins fused to transcription activation domain
  - When two proteins interact then corresponding gene is activated
  - Uetz, et al (2000), Nature, 403:623-627
- Affinity purification and mass spectroscopy
  - Protein -coding sequence is fused to a coding sequence of an affinity tag
  - Protein complexes are then purified and identified with gel electrophoresis and mass spectroscopy
  - Gavin, et al. (2002), Nature, 415:141-147
- Protein Microarrays
  - 2 types: antibody arrays, non-antibody arrays
  - Zhu, et al. (2001), Science, 293: 2101-2105

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Yeast two-hybrid system. From Griffiths, et al. *Modern Genetic Analysis* 

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First, we need accurate and high-throughput experimental techniques to gather the information necessary for the reconstruction. To date, there has not been much success in this field. However, recent reports indicate that there is increasing interest and efforts in this field. Here, we give two recent papers that detail protocols for determining the information that will are necessary for the reconstruction of signaling networks.

First, in a Feb. 2002, a group reported the use of polychromatic flow cytometry for measuring multiple active kinase states in a cell. In March 2002, another group reported the development of "phocuses," or genetically encoded fluorescent indicators, for visualizing phosphorylation in a cell. Here we see a schematic of how a "phocus" emits a different wavelength of light depending on the phosphorylation state of the substrate.

These approaches serve as representative examples of the experimental methods that are being developed and that are necessary to have the information necessary to reconstruct signaling networks.





With the necessary techniques beginning to surface, some work has been done to take the next step...the actual reconstruction. To date, most work has been limited to analyses at a small scale, i.e. analyzing the dynamics of a particular receptor-ligand complex. However, with the high degree of interconnection that exists in signaling networks, it is important to remember that such isolated studies have limited applicability.

One recent study made an attempt to look at a signaling network at a much broader scale. They analyzed the concentrations of 94 compounds after stimulation of the EGF receptor. The study accounted for rates of the various reactions before and after internalization of the EGF receptor. While the results of this one growth factor did present some interesting points, the analysis leads us to consider how one would model the entire signal transduction process of a cell. For such an analysis some important considerations have to be made.







# Current reconstruction efforts

#### nodes

# • Schuster et al. Eur. J. Biochem. 2002

- Review of models that analyze the role calcium plays in multiple signaling functions
- Kinetic analyses of multiple calcium concentrations



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- Alliance for Cellular Signaling
   www-signaling-gateway.org
- Multi-institutional effort to characterize all the signaling pathways in two model systems
  - B lymphocytes important for immunological function
  - Cardiac myocyte contractile cell of the heart
- Available data
  - Recent literature listing
    - Molecule pages
    - Comprehensive descriptions of proteins
  - Ligand Screens
    - Determine which inputs are important for cell physiology
    - Yeast-two hybrid screens
  - Describe protein-protein interactions

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With the necessary techniques beginning to surface, some work has been done to take the next step...the actual reconstruction. To date, most work has been limited to analyses at a small scale, i.e. analyzing the dynamics of a particular receptor-ligand complex. However, with the high degree of interconnection that exists in signaling networks, it is important to remember that such isolated studies have limited applicability.

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# A new generation of large-scale cellular models

- Data-driven
- Based on large organism-specific databases
- Scalable to whole-cell or genome-scale
- capable of integrating diverse experimental data types (genomic, transcriptomic, location analysis, proteomic, metabolomic, and phenomic data)
- Capable of accounting for inherent biological uncertainty

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The new generation of large and comprehensive models of complete cellular functions are: 1) data-driven, 2) based on large organism-specific databases, 3) scalable to whole-cell or genome-scale, 4) capable of integrating diverse experimental data types (genomic, transcriptomic, location analysis, proteomic, metabolomic, and phenomic data), and 5) capable of accounting for inherent biological uncertainty. It is important to note that these post-genomic era models are not expected to be able to compute cell functions with the same precision as we are used to in the disciplines of chemistry, physics, or engineering (i.e. the traditional "process"-type models based on the theory of reaction kinetics and other physico-chemical principles). These requirements necessitate a paradigm shift in the way large-scale in silico models are constructed.



To summarize this topic, we have basically covered three issues: first, metabolic networks can be reconstructed based on readily available genomic, biochemical and physiological information. These networks can be incorporated into genome-scale models which simulate cellular behavior, and the issues – false or missing reactions – may be addressed by building such models in an iterative process. Our next topic will be regulatory networks.

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